

# A Theory of Reference Point Formation

**Ozgur Kibris**  
Sabanci

**Yusufcan Masatlioglu**  
Maryland

**Elchin Suleymanov**  
Michigan

# Reference Dependence

- Markowitz [1952], Kahneman and Tversky [1979], and Tversky and Kahneman [1991]
- The idea of reference-dependence has played a very significant role in economics

# Reference Dependence

- Explain observed behavior such as
  - pension and insurance choice, selection of internet privacy, organ donation
  - Attitudes towards risk, equity premium puzzle, annuitization puzzle, disposition effect in financial markets and in housing markets
  - golf players, poker players, cab drivers, physicians, fishermen, deer hunters, drivers,...
  - Samuelson and Zeckhauser [1988], Kahneman Tversky [1984], Banford et al. [1979], Heberlein and Bishop [1985], Raymond and Hartman [1991], Boyce et al. [1992], Duborg et al. [1994], Kahneman et.al. [1990], Knetsch and Sinden [1984], Singh, [1991], Shogren et al. [1994], Morrison [1997], Coursey et al. [1987], Bateman et al. [1997], Johnson et al. [1993], Madrian and Shea [2001], Johnson et al. [2000], Johnson and Goldstein [2003],...
  - Thaler and Benartzi [2004], Sydnor [2010], Johnson et al [2002], Johnson-Goldstein [2003], Pope and Schweitzer [2011], Eil and Lien [2014], Camerer et al [1997], Rizzo and Zeckhauser [2003], Rabin [2000], Wakker [2010], Benartzi and Thaler [1995], Benartzi et al. [2011], Odean [1998], Genesove and Mayer [2001]...

# What is the reference point?

# What is the reference point?

- Markowitz [1952]

*It would be convenient if I had a formula [for the reference point].... But I do not have such a rule and formula.*

- Tversky and Kahneman [1991]

*The question of the origin and the determinants of the reference state lies beyond the scope of the present article.*

# What is the issue?

- Wakker [2010] argues that

*If too much liberty is left concerning the choice of reference points, then the theory becomes too general and is almost impossible to refute empirically.*

# A General Model

$$S \rightarrow r(S) \rightarrow \max_{x \in S} U_{r(S)}(x) \rightarrow c(S)$$

- $S$  and  $c(S)$  are observable
- $r(S)$  and  $\{U_\rho\}$  are not observable

# A General Model

$$S \rightarrow r(S) \rightarrow \max_{x \in S} U_{r(S)}(x) \rightarrow c(S)$$

- $S$  and  $c(S)$  are observable
- $r(S)$  and  $\{U_\rho\}$  are not observable
  
- Take  $r(S) = c(S)$  and  $U_\rho(\rho) > U_\rho(x)$  for all  $x \in X \setminus \rho$
- any choice can be rationalizable
- without any structure, there is no empirical content!!!
- reference point formation is the key



# Most Salient Alternative

- “Most salient alternative” as the reference point

Brickman, Coates, and Janoff-Bulman [1978], Samuelson and Zeckhauser [1988], Pratkanis [2007], DellaVigna [2009], Larrick and Wu [2012], Bhatia and Golman [2015], Bhatia [2017]

- Bhatia and Golman [2015]

*...reference points are merely options that are especially salient to the decision maker.*

# Our Aim

- We provide a simple theory of reference point formation
  - How the reference point endogenously determined
  - How it affects choices
  
- Based on the idea of most salient alternative

# Our Model

$$S \rightarrow r(S) \rightarrow \max_{x \in S} U_{r(S)}(x) \rightarrow c(S)$$

Choice  
Set

Most Salient  
Alternative

Reference-Dependent  
Utility Maximization

Choice

# Our Model

$$S \rightarrow r(S) \rightarrow \max_{x \in S} U_{r(S)}(x) \rightarrow c(S)$$

Choice  
Set

Most Salient  
Alternative

Reference-Dependent  
Utility Maximization

Choice

- $\gg$ : salience ranking
- $r(S)$ : the highest ranked alternative in  $S$  w.r.t.  $\gg$

Salience based Endogenous Reference Model (**SER**)

# Saliency Ranking

## Saliency ranking

- a reflection of what grabs the decision maker's attention
- subjective
- unobservable

# An Illustration

Consider a decision maker with a salient ranking

$$z \gg x \gg y$$

and reference-dependent utility functions

$$U_z(y) > U_z(z) > U_z(x) \text{ and } U_x(x) > U_x(y)$$

# An Illustration

Consider a decision maker with a salient ranking

$$z \gg x \gg y$$

and reference-dependent utility functions

$$U_z(y) > U_z(z) > U_z(x) \text{ and } U_x(x) > U_x(y)$$

Implied choices

# An Illustration

Consider a decision maker with a salient ranking

$$z \gg x \gg y$$

and reference-dependent utility functions

$$U_z(y) > U_z(z) > U_z(x) \text{ and } U_x(x) > U_x(y)$$

Implied choices

$S$	$\rightarrow$	$r(S)$	$\rightarrow$	$c(S)$
$\{x, y, z\}$		$z$		$y$
$\{x, y\}$		$x$		$x$
$\{y, z\}$		$z$		$y$
$\{x, z\}$		$z$		$z$



# Behavioral Patterns

SER accommodates

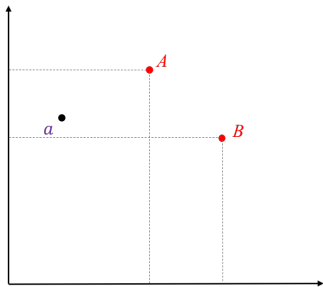
- Cyclical behavior
- Attraction Effect
- Compromise Effect
- More...

# Attraction Effect

- An inferior product increases the attractiveness of dominating another
- Huber, Payne, and Puto [1982]
- more than 7300 Google scholar articles

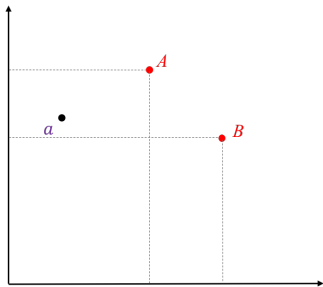
# Attraction Effect

- An inferior product increases the attractiveness of dominating another
- Huber, Payne, and Puto [1982]
- more than 7300 Google scholar articles



# Attraction Effect

- An inferior product increases the attractiveness of dominating another
- Huber, Payne, and Puto [1982]
- more than 7300 Google scholar articles

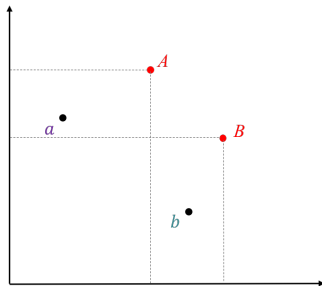


$$c(A, B) = B \text{ and } c(A, B, a) = A$$

# Attraction Effect

4-alternative version of AE

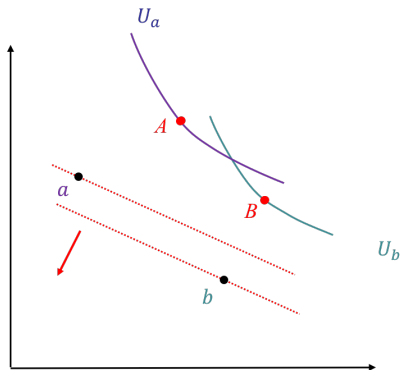
$$c(A, B, a) = A \text{ and } c(A, B, b) = B$$



# Attraction Effect

4-alternative version of AE

$$c(A, B, a) = A \text{ and } c(A, B, b) = B$$

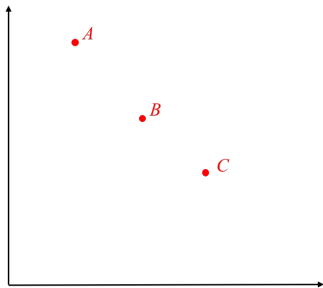


# Compromise Effect

- Tendency to choose the middle option
- Simonson [1989], Simonson and Tversky [1992]
- more than 2200 Google scholar articles

# Compromise Effect

- Tendency to choose the middle option
- Simonson [1989], Simonson and Tversky [1992]
- more than 2200 Google scholar articles



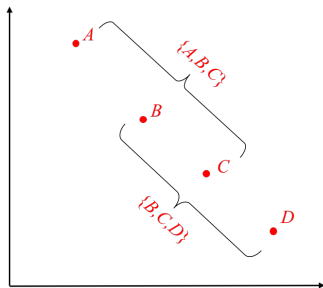
$$c(A, B, C) = B$$



# Compromise Effect

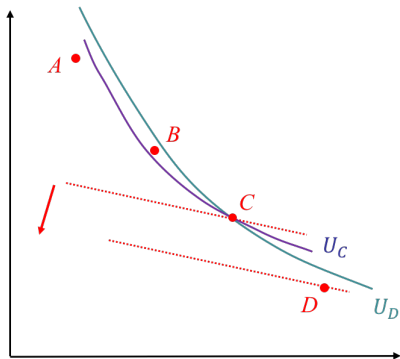
4-alternative version of CE

$$c(A, B, C) = B \text{ and } c(B, C, D) = C$$



# Compromise Effect

$$c(A, B, C) = B \text{ and } c(B, C, D) = C$$



# Prediction Power

- Is the model too general?

# Prediction Power

- Is the model too general?
- SER can be falsified.

# Prediction Power

- Is the model too general?
- SER can be falsified.
  - For example, the following  $c$  is outside of the model.

$S$	$c(S)$
$\{x, y, z\}$	$y$
$\{x, y\}$	$x$
$\{y, z\}$	$z$
$\{x, z\}$	$x$

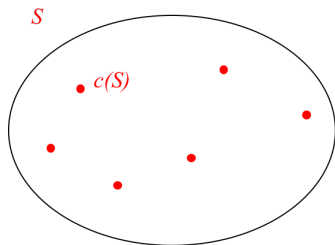
# Behavioral Foundation

# Behavioral Foundation

**Single Reversal Axiom:** For each  $S, T$  and distinct  $x, y$  with  $\{x, y\} \subseteq S \cap T$ ,

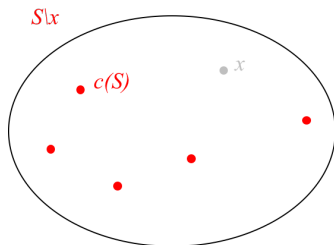
if  $x \neq c(S) \neq c(S \setminus x)$  and  $c(T) \neq y$  then  $c(T \setminus y) = c(T)$ .

# Single Reversal Axiom

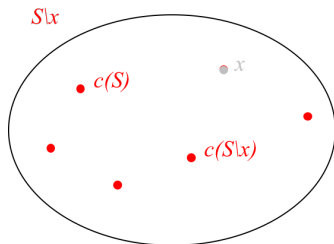




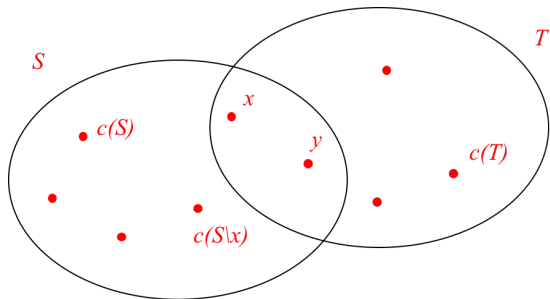
# Single Reversal Axiom



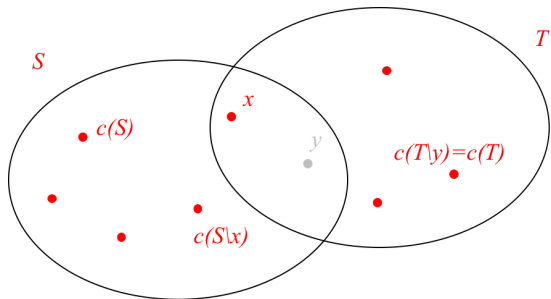
# Single Reversal Axiom



# Single Reversal Axiom



# Single Reversal Axiom



# Behavioral Foundation

## THEOREM

*A choice function  $c$  admits a SER representation if and only if it satisfies Single Reversal.*

# Uniqueness / Identification

a choice reversal  $\Rightarrow$  the reference point

# Uniqueness / Identification

a choice reversal  $\Rightarrow$  the reference point

$x \gg_R y$  if there is  $S \supseteq \{x, y\}$  such that  $x \neq c(S) \neq c(S \setminus x)$

# Uniqueness / Identification

a choice reversal  $\Rightarrow$  the reference point

$x \gg_R y$  if there is  $S \supseteq \{x, y\}$  such that  $x \neq c(S) \neq c(S \setminus x)$

## PROPOSITION

(**Revealed Salience**) Suppose  $c$  admits a SER representation. Then  $x$  is revealed to be more salient than  $y$  if and only if  $x \gg_R y$ .



# Uniqueness / Identification

- How to reveal preference between  $x$  and  $y$  when the reference point is  $z$ ?

# Uniqueness / Identification

- How to reveal preference between  $x$  and  $y$  when the reference point is  $z$ ?
  
- Find a choice problem such that
  - $x, y, z$  are feasible
  - $z$  is the reference point
  - $x$  is chosen

# Uniqueness / Identification

How to reveal preference between  $x$  and  $y$  when the reference point  $z$ ?

$xP_z y$  if there are  $S \supseteq T \supseteq \{x, y, z\}$  s.t.

$$(i) \quad z \neq c(S) \neq c(S \setminus z)$$

$$(ii) \quad x = c(T).$$

# Uniqueness / Identification

How to reveal preference between  $x$  and  $y$  when the reference point  $z$ ?

$xP_z y$  if there are  $S \supseteq T \supseteq \{x, y, z\}$  s.t.

$$(i) \quad z \neq c(S) \neq c(S \setminus z)$$

$$(ii) \quad x = c(T).$$

## PROPOSITION

(**Revealed Preference**) Suppose  $c$  admits a SER representation. Then  $x$  is revealed to be preferred to  $y$  under reference point  $z$  if and only if  $xP_z y$ .

# Summary

$$S \rightarrow r(S) \rightarrow \max_{x \in S} U_{r(S)}(x) \rightarrow c(S)$$

Choice  
Set

Most Salient  
Alternative

Reference-Dependent  
Utility Maximization

Choice

- an intuitive reference formation
- simple model
- simple axiomatization

# Psychological Constrained Model

# Psychological Constrained Model

A new underlying reference dependent choice (Masatlioglu and Ok [2014])

$$S \rightarrow r(S) \rightarrow \max_{x \in S \cap Q(r(S))} U(x) \rightarrow c(S)$$

# Psychological Constrained Model

A new underlying reference dependent choice (Masatlioglu and Ok [2014])

$$S \rightarrow r(S) \rightarrow \max_{x \in S \cap Q(r(S))} U(x) \rightarrow c(S)$$

- $r(S)$ : the most salient alternative in  $S$
- $U$ : reference-free
- Enable welfare analysis

Psychological Constrained SER (**PC-SER**)



# Behavioral Foundation

# Behavioral Foundation

**Consistency:** For each  $S \in \mathcal{X}$ , there is  $x \in S$  such that if  $\{x, z\} \subseteq T \subseteq T'$ ,  $z \neq c(T') \neq c(T' \setminus z)$  and  $x = c(x, z)$ , then either  $c(T) = x$  or  $c(T) \notin S$ .

# Behavioral Foundation

## THEOREM

*A choice function  $c$  admits a PC-SER representation if and only if it satisfies Single Reversal and Consistency.*

# Uniqueness / Identification

For any  $x, y, z$  such that  $x \neq y$ , we define

$xPy$  if  $\exists S, T$  with  $\{x, y, z\} \subseteq T \subseteq S$  such that

- (i)  $z \neq c(S) \neq c(S \setminus z)$ ,
- (ii)  $c(y, z) = y$ , and
- (iii)  $x = c(T)$ .

# Uniqueness / Identification

For any  $x, y, z$  such that  $x \neq y$ , we define

$xPy$  if  $\exists S, T$  with  $\{x, y, z\} \subseteq T \subseteq S$  such that

- (i)  $z \neq c(S) \neq c(S \setminus z)$ ,
- (ii)  $c(y, z) = y$ , and
- (iii)  $x = c(T)$ .

Let  $P^T$  be the transitive closure of  $P$ .

## PROPOSITION

(**Revealed Preference**) Suppose  $c$  admits a PC-SER representation. Then  $x$  is revealed to be preferred to  $y$  if and only if  $xP^T y$ .

# Uniqueness / Identification

$$Q_M(x) = \{y \in X \mid \exists S \supseteq T \supseteq \{x, y\} \text{ s.t. } x \neq c(S) \neq c(S \setminus x) \text{ and } y = c(T)\}$$

# Uniqueness / Identification

$$Q_M(x) = \{y \in X \mid \exists S \supseteq T \supseteq \{x, y\} \text{ s.t. } x \neq c(S) \neq c(S \setminus x) \text{ and } y = c(T)\}$$

## PROPOSITION

(**Revealed Psychological Constraint**) Suppose  $c$  admits a PC-SER representation. Then

- (i)  $x$  is revealed to be in the psychological constraint set of  $y$  iff  $x \in Q_M(y)$ ,
- (ii)  $x$  is revealed to be outside the psychological constraint set of  $y$  if and only if  $xP^T y$  and  $c(x, y) = y$ .

# Uniqueness / Identification

For any  $x \neq y$

- $x \gg_R y$  if (i)  $\exists S \supseteq \{x, y\}$  such that  $x \neq c(S) \neq c(S \setminus x)$ , or  
(ii)  $y P^T x$  and  $x = c(x, y)$ .

Let  $\gg_R^T$  stand for the transitive closure of  $\gg_R$ .



# Uniqueness / Identification

For any  $x \neq y$

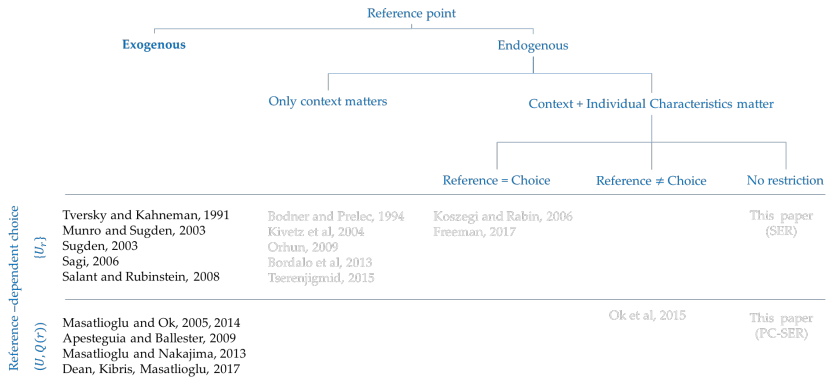
- $x \gg_R y$  if (i)  $\exists S \supseteq \{x, y\}$  such that  $x \neq c(S) \neq c(S \setminus x)$ , or  
(ii)  $y P^T x$  and  $x = c(x, y)$ .

Let  $\gg_R^T$  stand for the transitive closure of  $\gg_R$ .

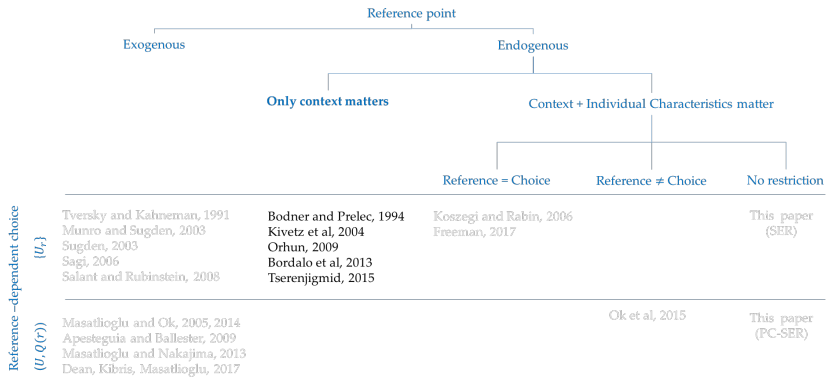
## PROPOSITION

(**Revealed Salience**) Suppose  $c$  admits a PC-SER representation. If  $x \gg_R^T y$  then  $x$  is revealed to be more salient than  $y$ .

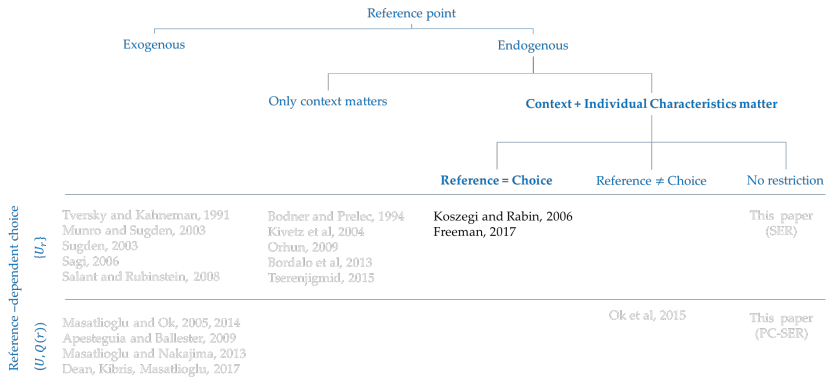
# Existing Literature



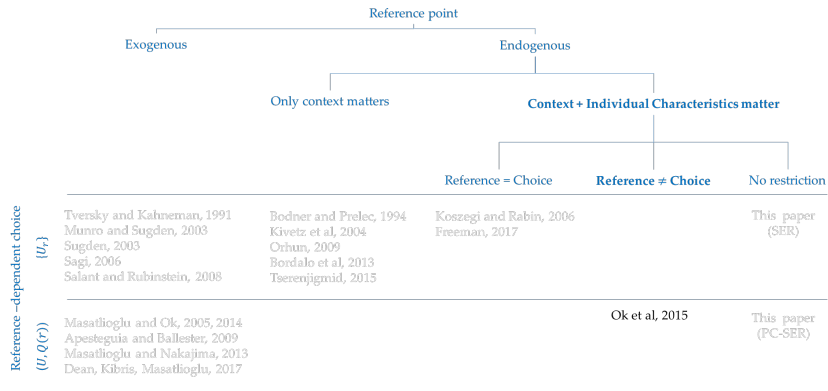
# Existing Literature



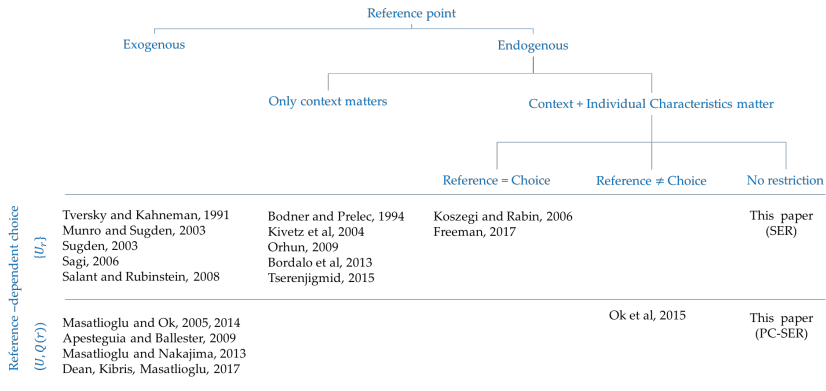
# Existing Literature



# Existing Literature



# Existing Literature



# A Comparison

- Consider riskless outcomes
- The constant loss aversion as the underlying reference-dependent model
- Consider two different reference point formations:
  - PPE (Koszegi and Rabin 2006)
  - Saliience Based (This paper)

# A Comparison

- The constant loss aversion model as the underlying reference-dependent model
- Consider two different reference point formations:
  - PPE (Koszegi and Rabin 2006)
  - Salience Based (This paper)



# A Comparison

- The constant loss aversion model as the underlying reference-dependent model
- Consider two different reference point formations:
  - PPE (Koszegi and Rabin 2006)
  - Saliency Based (This paper)

Answers

- WARP (hence No Compromise or Attraction Effects) (KR, 2006 Prop. 3)

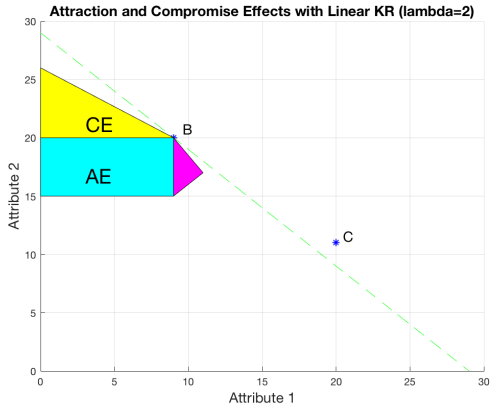
# A Comparison

- The constant loss aversion model as the underlying reference-dependent model
- Consider two different reference point formations:
  - PPE (Koszegi and Rabin 2006)
  - Salience Based (This paper)

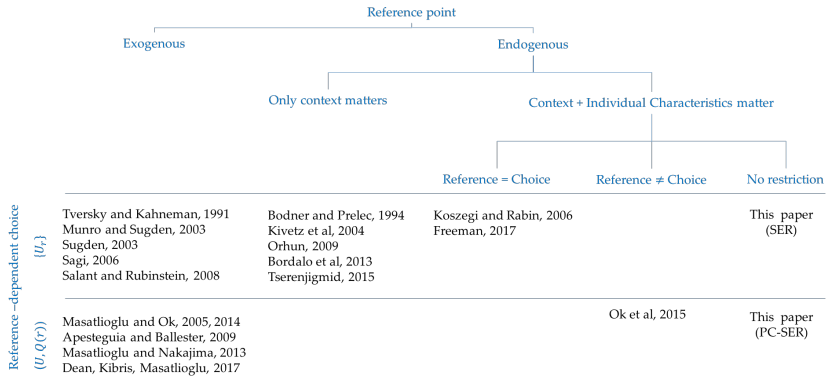
Answers

- WARP (hence No Compromise or Attraction Effects) (KR, 2006 Prop. 3)
- accommodates both Compromise and Attraction Effects

# A Comparison



# Conclusion



THANK YOU

- S. Bhatia. Comparing theories of reference-dependent choice. *Journal of Experimental Psychology: Learning, Memory, and Cognition*, 43(9):1490, 2017.
- S. Bhatia and R. Golman. Attention and reference dependence. *Working Paper*, 2015.
- P. Brickman, D. Coates, and R. Janoff-Bulman. Lottery winners and accident victims: Is happiness relative?. *Journal of Personality and Social Psychology*, 36(8):917 – 927, 1978. ISSN 0022-3514.
- S. DellaVigna. Psychology and economics: Evidence from the field. *Journal of Economic Literature*, 47(2):315–72, 2009.
- D. Kahneman and A. Tversky. Prospect theory: An analysis of decision under risk. *Econometrica*, 47(2):263–292, 1979.
- R. P. Larrick and G. Wu. Risk in negotiation: Judgments of likelihood and value. *Oxford University Press*, 2012.
- H. Markowitz. The utility of wealth. *Journal of Political Economy*, 60(2): 151–158, 1952.
- A. R. Pratkanis. Social influence analysis: An index of tactics. *The Science of Social Influence: Advances and Future Progress*, pages 17–82, 2007.
- W. Samuelson and R. Zeckhauser. Status quo bias in decision making. *Journal of Risk and Uncertainty*, 1(1):7–59, 1988.

- A. Tversky and D. Kahneman. Loss aversion in riskless choice: A reference-dependent model. *Quarterly Journal of Economics*, 106(4): 1039–1061, 1991.
- P. P. Wakker. *Prospect Theory: For Risk and Ambiguity*. Cambridge University Press, 2010.