

Department of Economics
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Economics 422
Midterm Examination

This exam contains 10 multiple-choice questions and two numerical/mathematical problems. You should try to do all questions and problems. Partial credit will be given for the numerical/mathematical problems, so please show all your work for these problems. **GOOD LUCK!**

Multiple-Choice Questions

1. (6 points) An estimator is

- (a) an estimate.
- (b) a formula that gives an efficient guess of the true population value.
- (c) a random variable.
- (d) a nonrandom number.

2. (6 points) The p -value associated with testing the null hypothesis

$$H_0 : \mu_Y = 5$$

against the alternative hypothesis

$$H_0 : \mu_Y \neq 5$$

is defined as follows:

- (a) $p = 0.05$
- (b) $\Pr_{H_0} \left[|\bar{Y} - 5| > \left| \bar{Y}^{act} - 5 \right| \right]$.
- (c) $\Pr [Z > 1.96]$, where $Z \sim N(0, 1)$.
- (d) $\Pr_{H_0} \left[|\bar{Y} - 5| < \left| \bar{Y}^{act} - 5 \right| \right]$.

3. (6 points) An estimator $\hat{\mu}_Y$ of the population value μ_Y is consistent if

- (a) $\hat{\mu}_Y \xrightarrow{p} \mu_Y$.
- (b) its mean square error is the smallest possible.
- (c) Y is normally distributed.
- (d) $\bar{Y} \xrightarrow{p} 0$.

4. (6 points) The t -statistic for testing the null hypothesis

$$H_0 : \mu_Y = 1$$

against the alternative hypothesis

$$H_0 : \mu_Y \neq 1$$

is defined as follows:

(a) $t = \frac{\bar{Y}-1}{\sigma_Y^2/n}$.

(b) $t = \frac{\bar{Y}-1}{SE(\bar{Y})}$.

(c) $t = \frac{(\bar{Y}-1)^2}{SE(\bar{Y})}$

(d) 1.96.

5. (6 points) A large p -value implies

(a) rejection of the null hypothesis.

(b) a large t -statistic.

(c) a large \bar{Y}^{act} .

(d) that the observed value \bar{Y}^{act} is consistent with the null hypothesis.

6. (6 points) The standard error of the regression (SE_R) for the simple linear model

$$Y_i = \beta_0 + \beta_1 X_i + u_i, \quad i = 1, \dots, n,$$

is defined as follows:

(a) $\sqrt{\frac{1}{n-2} \sum_{i=1}^n \widehat{u}_i^2}$

(b) SSR

(c) $1 - R^2$

(d) $\sqrt{\frac{1}{n-1} \sum_{i=1}^n \widehat{u}_i^2}$

Here, \widehat{u}_i ($i = 1, \dots, n$) denote the OLS residuals.

7. (6 points) The following are all least squares assumptions with the exception of

- (a) The conditional distribution of u_i given X_i has a mean of zero with probability one.
- (b) The explanatory variable in the regression model is normally distributed.
- (c) (X_i, Y_i) , $i = 1, \dots, n$ are independent and identically distributed.
- (d) Large outliers are unlikely.

8. (6 points) Which of the following statements is correct?

- (a) $TSS = ESS + SSR$
- (b) $ESS = SSR + TSS$
- (c) $ESS > TSS$
- (d) $R^2 = 1 - (ESS/TSS)$

9. (6 points) The OLS estimator is derived by

- (a) connecting the Y_i corresponding to the lowest X_i observation with the Y_i corresponding to the highest X_i observation.
- (b) making sure that the standard error of the regression equals the standard error of the slope estimator.
- (c) minimizing the sum of absolute residuals.
- (d) minimizing the sum squared residuals.

10. (6 points) The normal approximation to the sampling distribution of $\hat{\beta}_1$ is powerful because

- (a) many explanatory variables in real life are normally distributed.
- (b) it allows econometricians to develop methods for statistical inference without explicitly knowing the underlying distribution of the data.
- (c) many other distributions are not symmetric.
- (d) implies that OLS has small variance.

Problems:

11. (20 points)

Suppose you are interested in how well one's height predicts one's weight. Hence, you collect data on 110 people in order to run the simple regression

$$Y_i = \beta_0 + \beta_1 X_i + u_i, \quad i = 1, \dots, 110;$$

where Y_i denotes the weight of the i^{th} individual and X_i denotes the height of the i^{th} individual. From this data, you calculated the following quantities:

$$\begin{aligned} \sum_{i=1}^{110} Y_i &= 17,375, & \sum_{i=1}^{110} (Y_i - \bar{Y})^2 &= 94,228.8, \\ \sum_{i=1}^{110} X_i &= 7665.5, & \sum_{i=1}^{110} (X_i - \bar{X})^2 &= 1248.9, \\ \sum_{i=1}^{110} (X_i - \bar{X})(Y_i - \bar{Y}) &= 7625.9 \end{aligned}$$

where \bar{Y} and \bar{X} denote the respective sample means.

- (a) From the information given above, calculate the OLS estimates for β_0 and β_1 . Show your work.
- (b) Calculate the (unadjusted) R^2 measure for this regression and explain its meaning. Show your work.

12. (20 points)

Suppose you have the random sample

$$X_1, X_2, \dots, X_n \sim i.i.d. (\mu_X, 4)$$

Consider the statistic

$$S_n = \sqrt{n} \bar{X}_n,$$

where

$$\bar{X}_n = \frac{1}{n} \sum_{i=1}^n X_i.$$

- (a) What is the approximate distribution of S_n under the null hypothesis that $\mu_X = 0$, when the sample size n is large? Explain how you have arrived at your answer.
- (b) Calculate an approximate value for the probability

$$\Pr [-1.25 \leq \bar{X}_n - 1 \leq -0.5]$$

under the null hypothesis that $\mu_X = 0$, when $n = 100$. Show your work.