

# Discussion of Wu and Zhang

S. Borağan Aruoba  
University of Maryland

October 15, 2016

Chicago Fed DSGE Conference

# Summary

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
  - All “problems” due to the reality of the central bank to reach: multiplicity of equilibria, long multiplicity, multiple regimes, ...
  - ... and the model solving is an illusion.
- Let’s confront these assumptions with U.S. data. (ultimate goal is to estimate this model)

# Summary

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
    - New regime with new tools? (Balance sheet, forward guidance, ...)
  - Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
  - **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
    - All “standard” due to the reality of the central bank to react: multiplicity of equilibria, multiple steady states, non-stochastic steady state, and the model solving in an instant.
  - Let's confront these assumptions with U.S. data. (ultimate goal is to estimate this model)

# Summary

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
  - All “standard” assumptions: validity of the Taylor rule to reach multiplicity of equilibria, multiplicity of equilibria, and the model solving by an interest rate.
- Let's confront these assumptions with U.S. data. (ultimate goal is to estimate this model)

# Summary

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
  - All “problems” due to the inability of the central bank to react: multiplicity of equilibria, large multipliers, strange responses, ...
  - ... and the model solves its own problems.
- Let’s confront these assumptions with U.S. data. (ultimate goal is to estimate this model)

# Summary

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
  - All “problems” due to the inability of the central bank to react: multiplicity of equilibria, large multipliers, strange responses.
  - ... and the model solves in an instant.
- Let's confront these assumptions with U.S. data. (ultimate goal is to estimate this model)

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
  - All “problems” due to the inability of the central bank to react: multiplicity of equilibria, large multipliers, strange responses.
  - ... and the model solves in an instant.
- Let's confront these assumptions with U.S. data. (ultimate goal is to estimate this model)

# Summary

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
  - All “problems” due to the inability of the central bank to react: multiplicity of equilibria, large multipliers, strange responses.
  - ... and the model solves in an instant.
- Let's confront these assumptions with U.S. data. (ultimate goal is to estimate this model)



- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
  - All “problems” due to the inability of the central bank to react: multiplicity of equilibria, large multipliers, strange responses.
  - ... and the model solves in an instant.
- Let’s confront these assumptions with U.S. data. (ultimate goal is to estimate this model)

- ① Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.

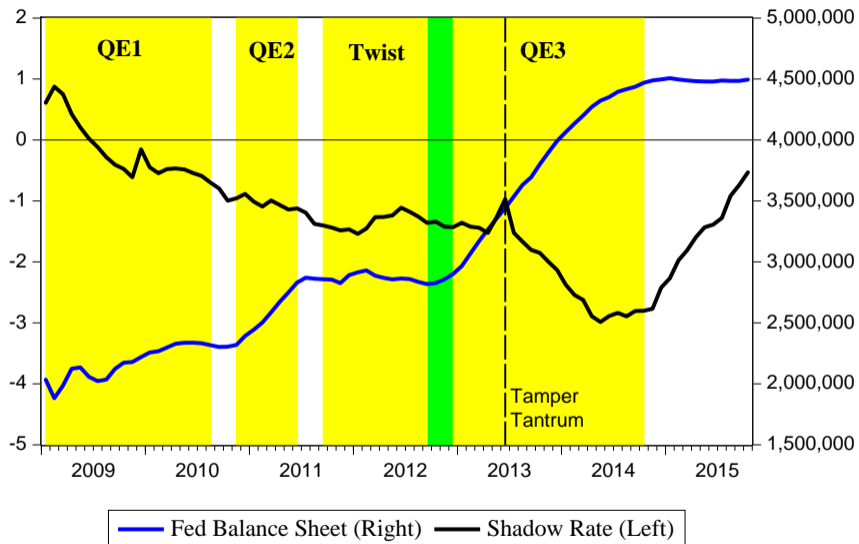
# Assumption 1: Shadow rate reacts to events like FFR

	Change in Policy (monthly, in bp)		
	1998-2008	1998-2015	2009-2015
Initial Claims Surprises (lagged, std)	-10.9 (**)	-11.1 (**)	-0.5
Initial Claims Surprises $\times$ ZLB		10.0 (**)	

- ① Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.

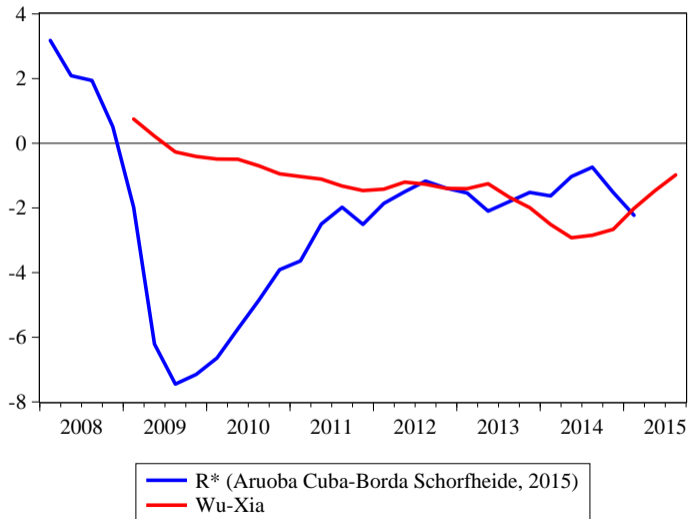
- ① Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- ② Shadow rate is a good description of Fed's unconventional policies.

# Assumption 2: Shadow Rate Captures UMP



# Assumption 2: Shadow Rate Captures UMP

Was the Fed policy not nearly expansionary as it should be in 2009-2010?

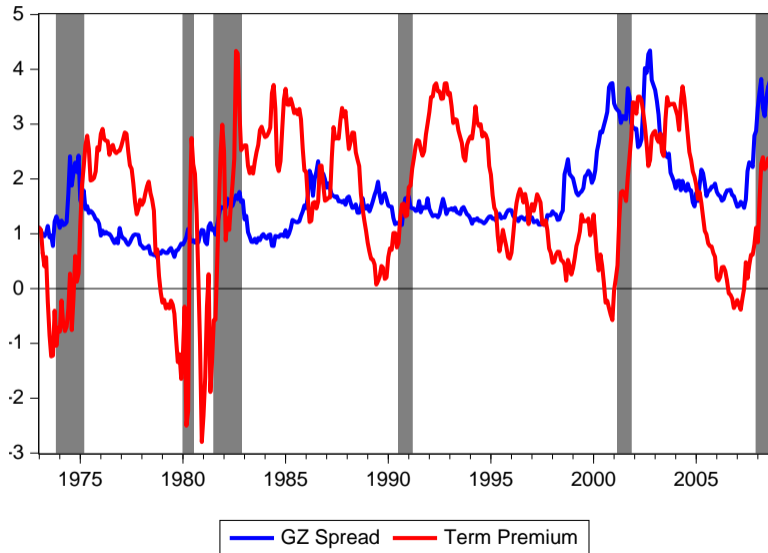


- ① Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- ② Shadow rate is a good description of Fed's unconventional policies.
  - Broadly, maybe, but at more high frequency, it is not clear.

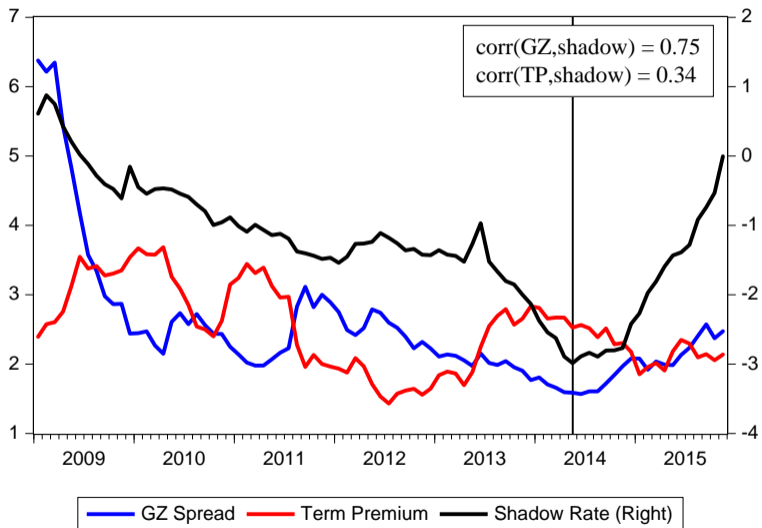


- ① Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- ② Shadow rate is a good description of Fed's unconventional policies.
  - Broadly, maybe, but at more high frequency, it is not clear.
- ③ Risk premium / term premium is constant away from ZLB and is linear in the shadow rate at ZLB.

# Assumption 3: Risk/Term Premium at and away from ZLB

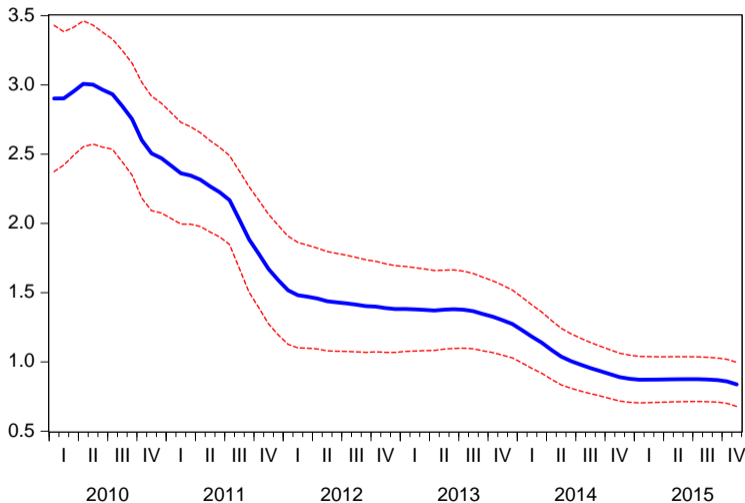


# Assumption 3: Risk/Term Premium at and away from ZLB



# Assumption 3: Risk/Term Premium at and away from ZLB

Estimate  $spread_t = \alpha + \beta_T s_t + \epsilon_t$  for  $t = 1, \dots, T$  recursively and plot  $\beta_T$ .



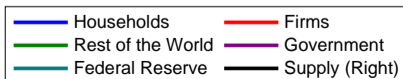
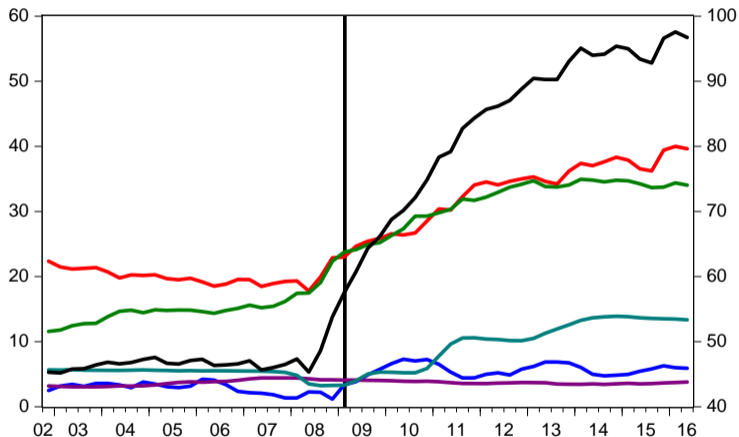
- 1 Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- 2 Shadow rate is a good description of Fed's unconventional policies.
  - Broadly, maybe, but at more high frequency, it is not clear.
- 3 Risk premium / term premium is constant away from ZLB and is linear in the shadow rate at ZLB.
  - Risk premium moves endogenously away from ZLB, link to shadow is not stable.

# Assumptions and U.S. Data

- 1 Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- 2 Shadow rate is a good description of Fed's unconventional policies.
  - Broadly, maybe, but at more high frequency, it is not clear.
- 3 Risk premium / term premium is constant away from ZLB and is linear in the shadow rate at ZLB.
  - Risk premium moves endogenously away from ZLB, link to shadow is not stable.
- 4 Bond holdings of the public is constant away from ZLB and it is linear in the shadow rate at ZLB (i.e. it falls as  $s_t$  falls below zero)

# Assumption 4: Government Bonds at and away from ZLB

## Supply and Demand for U.S. Government Bonds (% of GDP)



# Assumptions and U.S. Data

- 1 Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- 2 Shadow rate is a good description of Fed's unconventional policies.
  - Broadly, maybe, but at more high frequency, it is not clear.
- 3 Risk premium / term premium is constant away from ZLB and is linear in the shadow rate at ZLB.
  - Risk premium moves endogenously away from ZLB, link to shadow is not stable.
- 4 Bond holdings of the public is constant away from ZLB and it is linear in the shadow rate at ZLB (i.e. it falls as  $s_t$  falls below zero)
  - Fiscal response to crisis / flight to quality increases both supply and holdings of government bonds by the public. Fed's share (still) small.



# Assumptions and U.S. Data

- 1 Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- 2 Shadow rate is a good description of Fed's unconventional policies.
  - Broadly, maybe, but at more high frequency, it is not clear.
- 3 Risk premium / term premium is constant away from ZLB and is linear in the shadow rate at ZLB.
  - Risk premium moves endogenously away from ZLB, link to shadow is not stable.
- 4 Bond holdings of the public is constant away from ZLB and it is linear in the shadow rate at ZLB (i.e. it falls as  $s_t$  falls below zero)
  - Fiscal response to crisis / flight to quality increases both supply and holdings of government bonds by the public. Fed's share (still) small.
- 5 Key variables such as output and inflation behave at ZLB just like they do away from ZLB, i.e. they do not inherit the ZLB kink.

## Assumption 5: Key Variables at and Away from ZLB

<b>Moment</b>	<b>Pre-ZLB (1984-2008)</b>	<b>ZLB (2009-2015)</b>
$\text{corr}(\pi_t, \pi_{t-1})$	0.48	0.40
$\text{corr}(y_t, y_{t-1})$	0.34	0.08
$\text{corr}(y_t, \pi_t)$	-0.17	0.24
$\text{corr}(R_t, y_t)$	0.06	-0.42
$\text{corr}(R_t, \pi_t)$	0.18	-0.22

# Assumptions and U.S. Data

- 1 Shadow rate reacts to events (e.g. to output and inflation deviations) just the way FFR does.
  - Shadow rate shows a muted response to news.
- 2 Shadow rate is a good description of Fed's unconventional policies.
  - Broadly, maybe, but at more high frequency, it is not clear.
- 3 Risk premium / term premium is constant away from ZLB and is linear in the shadow rate at ZLB.
  - Risk premium moves endogenously away from ZLB, link to shadow is not stable.
- 4 Bond holdings of the public is constant away from ZLB and it is linear in the shadow rate at ZLB (i.e. it falls as  $s_t$  falls below zero)
  - Fiscal response to crisis / flight to quality increases both supply and holdings of government bonds by the public. Fed's share (still) small.
- 5 Key variables such as output and inflation behave at ZLB just like they do away from ZLB, i.e. they do not inherit the ZLB kink.
  - Some key correlations seems to change signs.

- Major challenge: In 2020, how are we going to estimate our models with data covering 2009-2015?
  - Continuous regime with ZLB?
  - New regime with new tools? (Balance sheet, forward guidance, ...)
- Either way, take regime change and/or occasionally-binding constraints seriously when solving/estimating models.
- **This paper:** Take your favorite DSGE model, replace FFR that is subject to the ZLB constraint with the shadow rate and solve the model linearly. All will be well. (**need to accept some assumptions**)
- This approach is not (yet) ready for prime-time.
  - If we were to estimate it using U.S. data covering 2009-2015, it would not do well.
- Looking forward to the next iteration.